

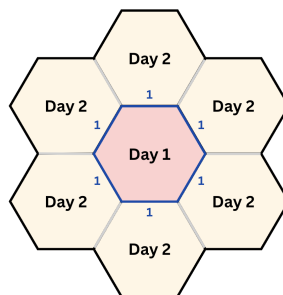
Problem 1.1: Barbie the Bee is collecting honey from 100 distinct flowers labeled from 1 to 100. She visits a given flower if and only if all the digits of the flower are distinct and the flower is not even-numbered. How many flowers does she visit?

Problem 1.2: Let $T = \text{TNYWR}$. All bees in a certain colony have body patterns made up of n stripes, where n is the remainder when T is divided by 10. Each stripe is black or yellow, and every bee's stripe pattern is not equal to its reverse. What's the maximum number of unique stripe patterns in such a bee colony?

(e.g. $(BYBY)$ is a good stripe pattern as $(YBYB)$ is its reverse, but $(YBBY)$ is not, as $(YBBY)$ is its reverse)

Problem 1.3: Let $T = \text{TNYWR}$. Barbie the Bee is building a honeycomb structure. On day 1, she builds a hexagonal honeycomb with side length 1. On each subsequent day, she covers the entire perimeter of the existing honeycomb with hexagons of side length 1. The resulting structure after day 2 is shown below. What's the perimeter of Barbie's honeycomb after T days (the perimeter is just the length of the exterior of the entire honeycomb)?

(i.e. after Day 1, the honeycomb will have a perimeter of 6 while after Day 2, the honeycomb will have a perimeter of 18)



Barbie's honeycomb after 2 days

Problem 2.1: In triangle DEF , there is a point U on \overline{DF} and a point K on \overline{EF} such that K is the midpoint of \overline{EF} . If the area of quadrilateral $DUKE$ is 12 and the area of triangle KUF is 2, the ratio $\frac{DF}{DU}$ can be expressed as $\frac{m}{n}$, where m and n are relatively prime positive integers. Find $m + n$.

Problem 2.2: Let $T = \text{TNYWR}$, and $p = \frac{T-2}{T+2}$. Duke is in a close basketball game with their rival UNC. The current score is 67-66 in Duke's favor, and there are 3 minutes left in the game. After each minute, Duke outscores UNC by 1 point with probability p and UNC outscores Duke by 1 point with probability $1 - p$. Given that each scoring update is independent of all previous scoring updates, the probability that Duke is winning when the game is over can be expressed as $\frac{m}{n}$, where m and n are relatively prime positive integers. Find $1000m + n$.

Problem 2.3: Let $T = \text{TNYWR}$. Let K be the units digit of T . The Duke Blue Devil mascot loves to stack donuts on the three prongs of his trident. If he receives K distinct donuts, how many ways can he arrange them on his trident? Note that the order in which he places the donuts on each prong matters.